



# Tapered Hollow-Core Fibers Providing Single-mode Output in the $3.5 \mu\text{m} - 7.8 \mu\text{m}$ Spectral Range

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# Outline

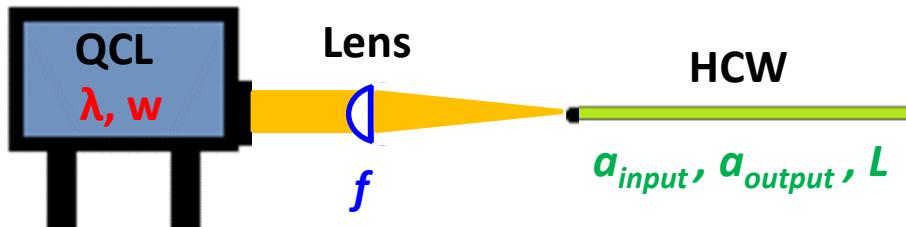
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- **Introduction**
- **Theoretical model**
- **Experimental results**
- **Conclusions**

## Hollow-Core Waveguides

$$a(z) = \frac{a_{output} - a_{input}}{L} z + a_{input}$$

# Collimated Laser Beam-HCW Optical Coupling



- Diffraction-limited collimated Gaussian beam

- Focal length: 
$$f = \frac{R}{1 + \left( \frac{\lambda R}{\pi w^2} \right)^2}$$

- Waist radius at the focal plane: 
$$w_0 = \sqrt{\frac{w}{1 + \left( \frac{\pi w^2}{\lambda R} \right)^2}}$$

- Beam intensity distribution: 
$$G(r) = G_0 e^{-\frac{r^2}{w_0^2}}$$

# Coupling efficiency

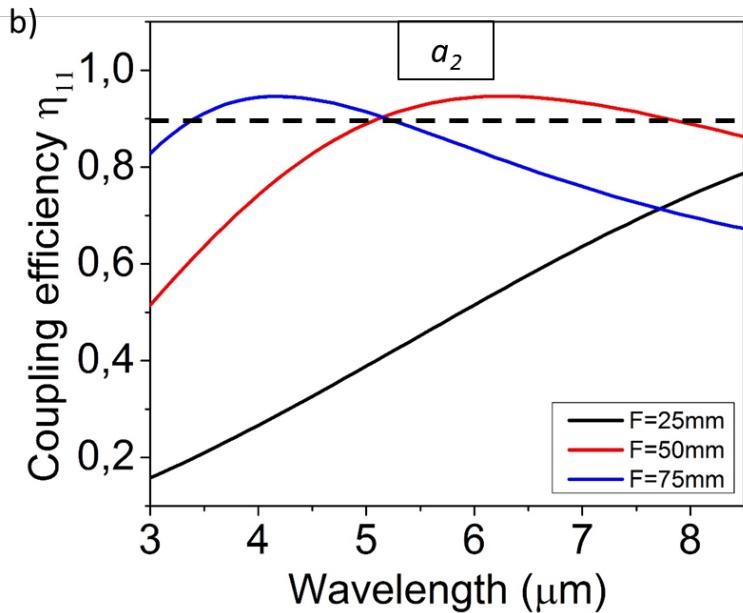
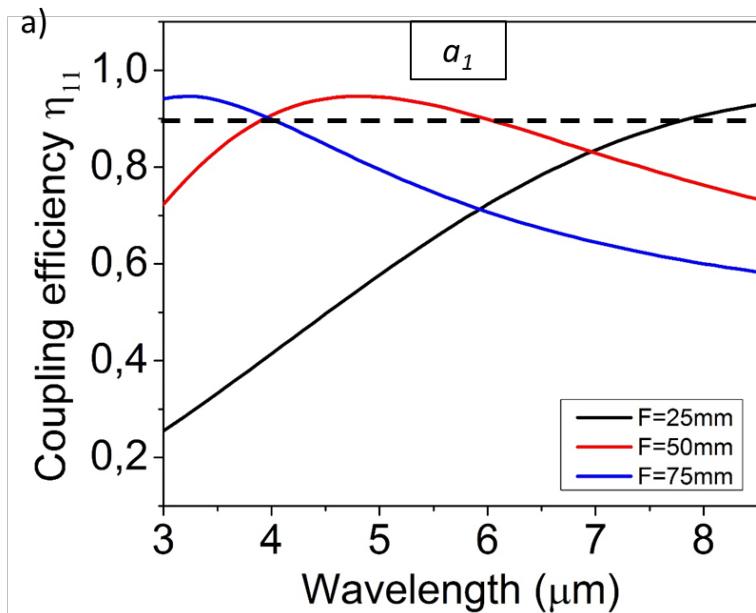
- HCW hybrid modes: zero-order Bessel functions:

$$J\left(u_{1m} \frac{r}{a_{input}}\right)$$

- Power coupling efficiency:

$$\eta_{1m} = \frac{\left| \int_0^{a_{input}} G(r) J\left(u_{1m} \frac{r}{a_{input}}\right) r dr \right|^2}{\int_0^{a_{input}} G(r) r dr \int_0^{a_{input}} J\left(u_{1m} \frac{r}{a_{input}}\right) r dr}$$

Depends only on  $a_{input}$



# Propagation Losses

- **Attenuation coefficient:**

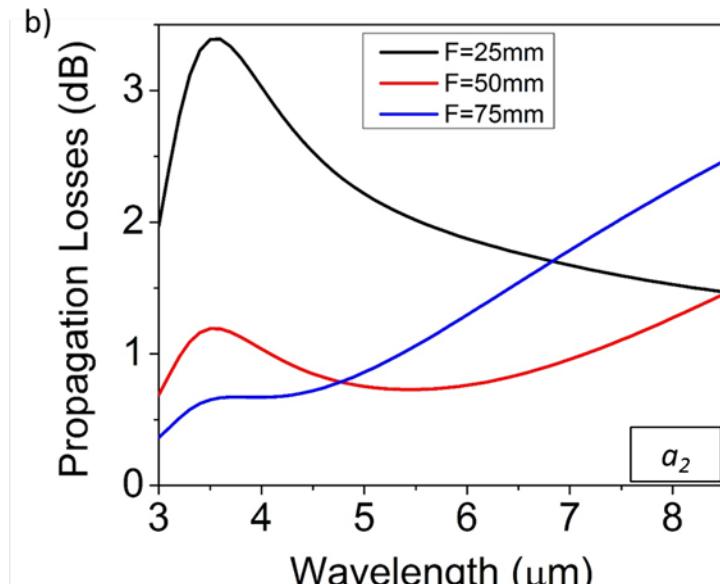
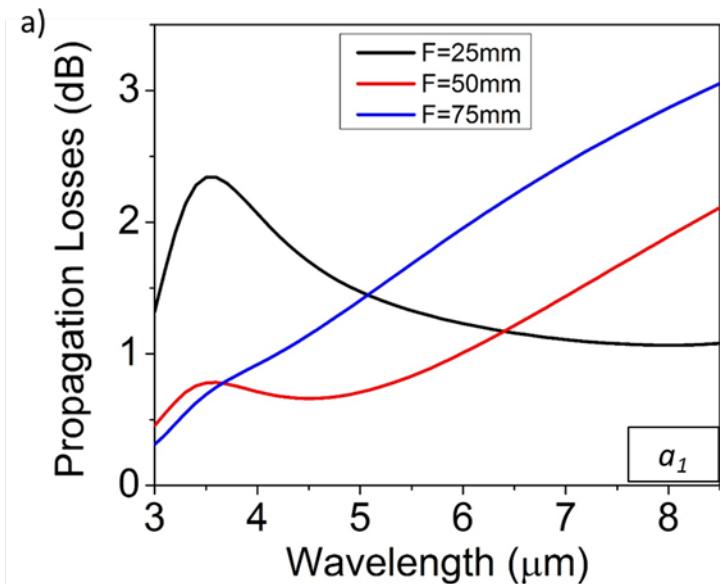
$$\alpha_{1m} = \left( \frac{u_{1m}}{2\pi} \right)^2 \frac{\lambda^2}{a(z)^3} \frac{n}{n^2 + k^2} \frac{1}{2} \left( 1 + \frac{n_d^2}{\sqrt{n_d^2 - 1}} \right)^2 = K \frac{u_{1m}^2 \lambda^2}{a(z)^3}$$

- **Theoretical Losses:**

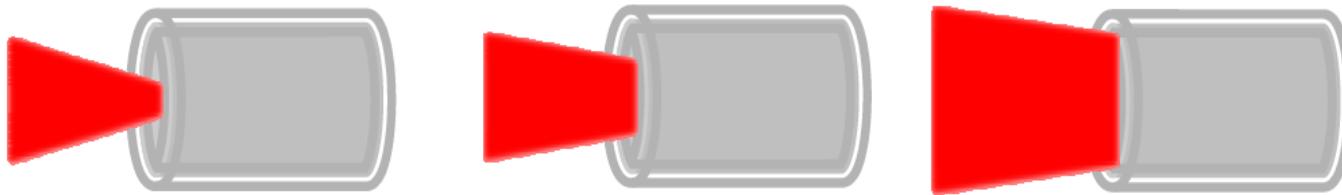
$$L_p(dB) = -10 \log_{10} \left( \sum_m \eta_{1m} \exp \left( -2 \int_0^L \alpha_{1m}(z) dz \right) \right)$$

$$-10 \log_{10} \left( \sum_m \eta_{1m} \exp \left( -2 K u_{1m}^2 \lambda^2 L \frac{a_{input} + a_{output}}{2 a_{input} a_{output}} \right) \right)$$

Depends both on  $a_{input}$  and  $a_{output}$



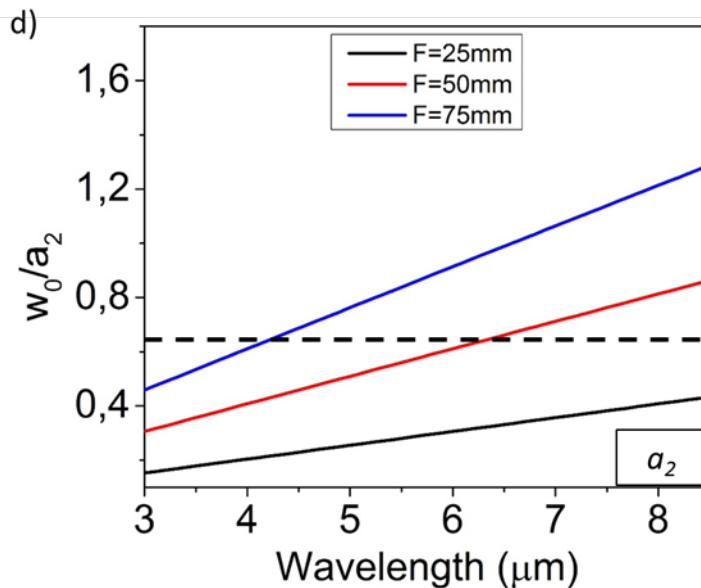
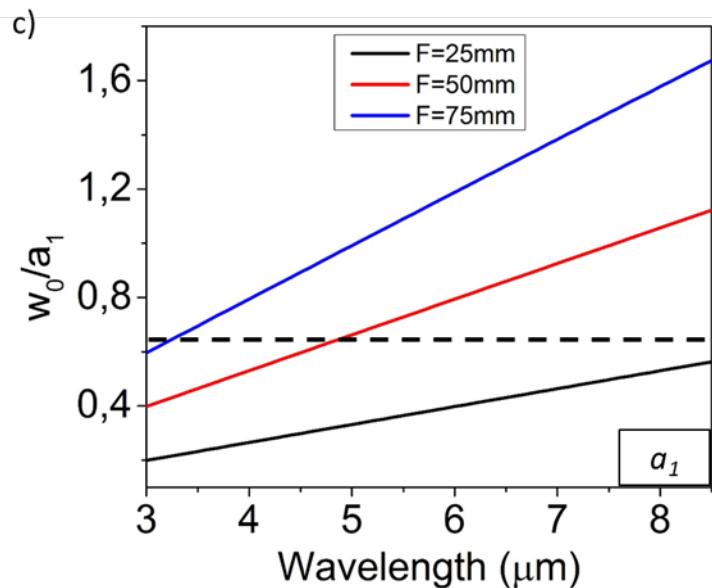
# $w_0/a_{input}$ Parameter



Under-fill:  
Excite higher order modes

$w_0/a=0.64$   
Optimal coupling

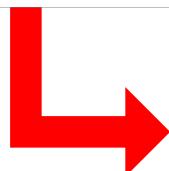
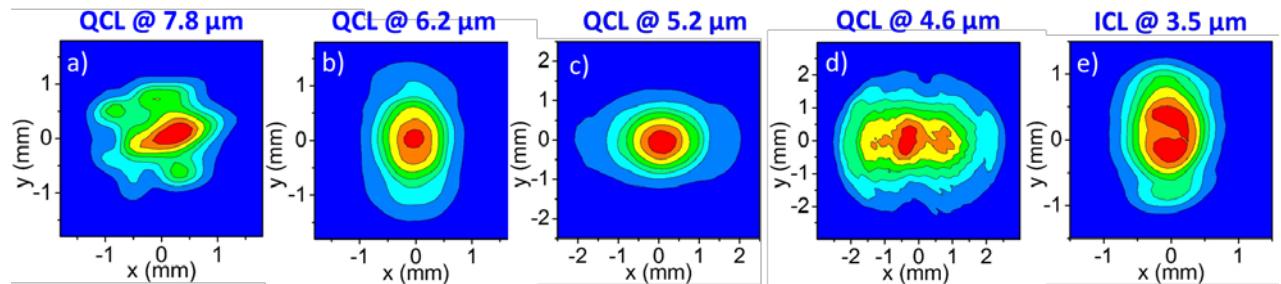
Over-fill:  
Beam is clipped



# Experimental Setup

## Optical coupling with five lasers in the mid-IR spectral range

Beam profiles  
acquired at the  
lasers exit

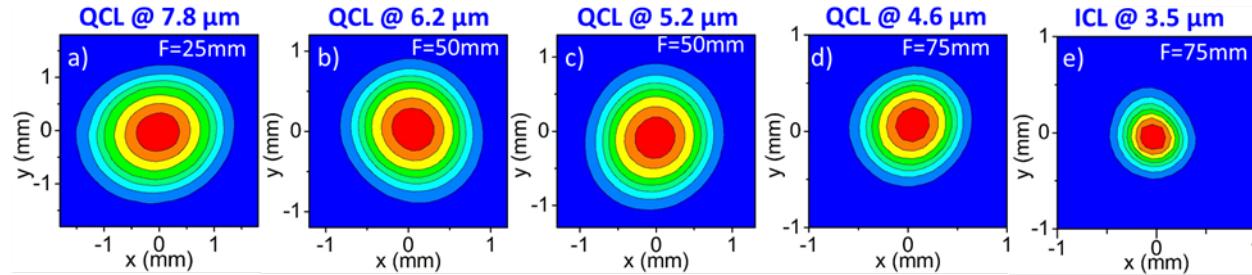
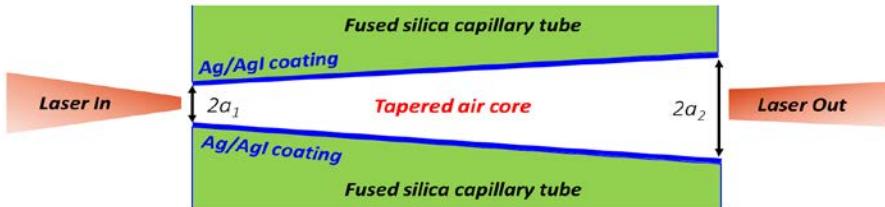


Focal lengths providing the best coupling conditions

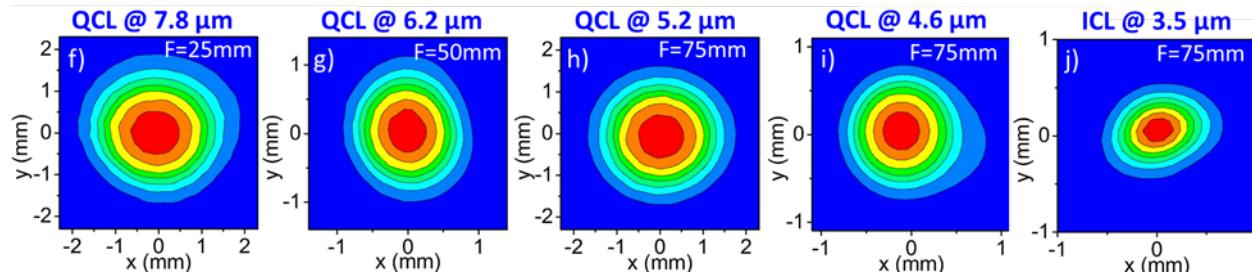
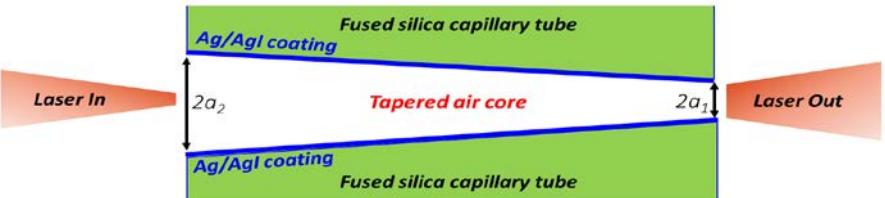
		7.8 $\mu\text{m}$ QCL	6.2 $\mu\text{m}$ QCL	5.2 $\mu\text{m}$ QCL	4.6 $\mu\text{m}$ QCL	3.5 $\mu\text{m}$ ICL
$a_1$	$f$	25 mm	50 mm	50 mm	75 mm	75 mm
	$\eta_{II}$	89.6%	88.6%	94.0%	83.6%	93.8%
	$w_0/a_1$	0.52	0.82	0.69	0.91	0.70
$a_2$	$f$	25 mm	50 mm	75 mm	75 mm	75 mm
	$\eta_{II}$	72.2%	94.6%	89.9%	93.6%	91.1%
	$w_0/a_2$	0.40	0.63	0.80	0.70	0.54

# Beam Profiles at Tapered-HCW Exit

## ○ Input bore radius: $a_1$



## ○ Input bore radius: $a_2$



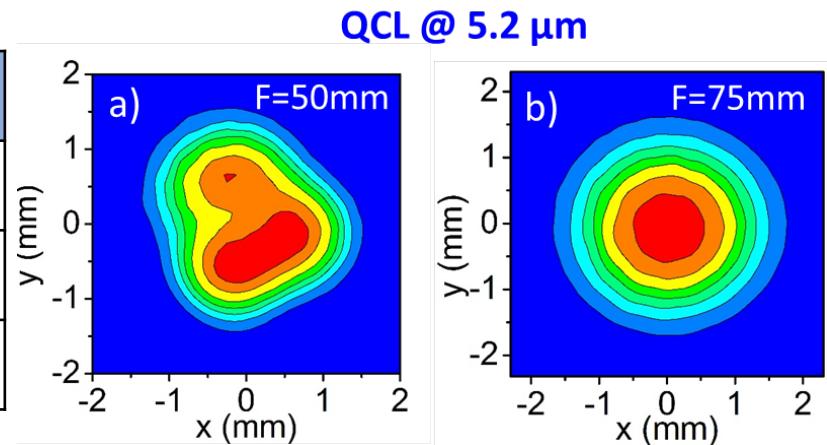
Single mode output when  $a_1$  or  $a_2$  as input bore radius

# Influence of $w_0/a$ Parameter on the Beam Quality

Example of 5.2  $\mu\text{m}$  QCL coupled into input bore radius  $a_2$

- $F = 50 \text{ mm}$  and  $F = 75 \text{ mm}$  allowing the same coupling efficiency of the laser power with the  $J_{11}$  mode

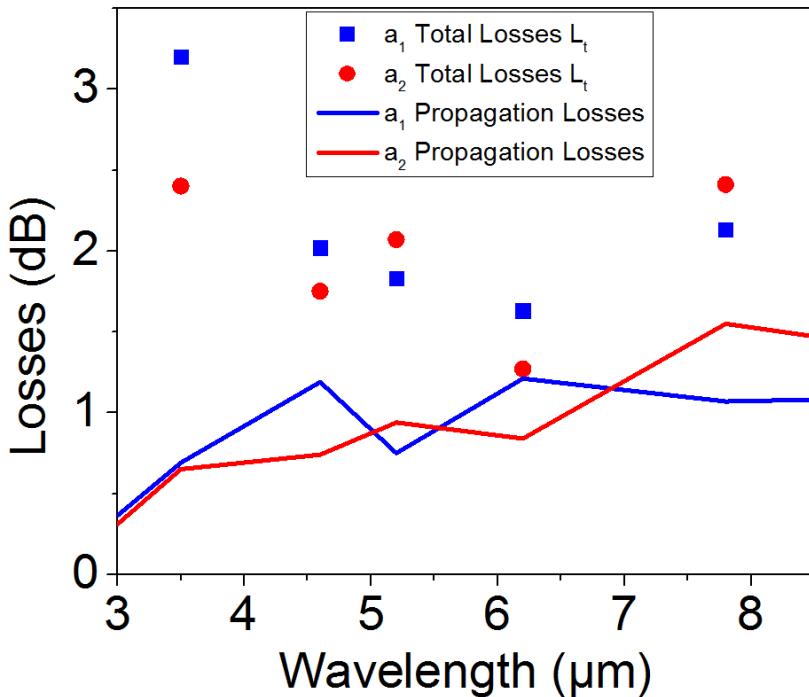
$f$	50 mm	75 mm
$\eta_{11}$	90.1%	90 %
Propagation Losses	74 dB	93 dB
$w_0/a_1$	<b>0.53</b>	<b>0.80</b>



Although 90% coupling efficiencies, a  $w_0/a_2$  value substantially lower than 0.64 does not guarantee a single-mode output

# Total Losses vs Theoretical Losses

- Experimental Total Losses



$$L_t (\text{dB}) = -10 \log_{10} \frac{P_{out}}{P_{in}}$$

For each laser, lower losses when using the input side  $a_i$  giving the larger  $\eta_{11}$

Discrepancy ascribed to

- low spatial quality of the laser beams
- at  $3.5 \mu\text{m}$ : scattering losses  $\propto 1/\lambda^2$ , caused by HCW inner surface roughness

# Conclusions

- Study on the influence of  $f$ ,  $\lambda$  and  $a$  on Tapered-HCW performance
- Theoretical model predicting the best operating conditions for single-mode output and low optical losses
- Experimental validation of the model in the  $3.5\text{-}7.8 \mu\text{m}$  spectral range
- Selection of the coupling inner bore  $a$ , allowing single-mode output with the lowest losses

	7.8 $\mu\text{m}$ QCL	6.2 $\mu\text{m}$ QCL	5.2 $\mu\text{m}$ QCL	4.6 $\mu\text{m}$ QCL	3.5 $\mu\text{m}$ ICL
$f$	25 mm	50 mm	50 mm	75 mm	75 mm
$2w$	1.9 mm	2.3 mm	2.8 mm	3.5 mm	1.9 mm
A	$a_1$	$a_2$	$a_1$	$a_2$	$a_2$
$\eta_{11}$	89.6%	94.6%	94.0%	93.6%	91.1%
$w_0/a$	0.52	0.63	0.69	0.70	0.54
$L_t$ (dB)					
Beam Profile					